

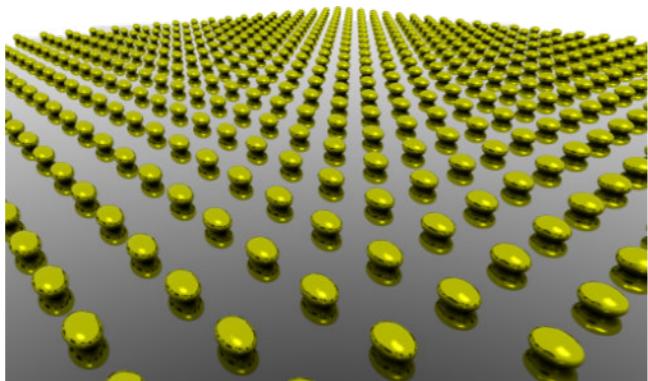
# COUPLED DIPOLE SIMULATIONS OF LIGHT SCATTERING BY MOLECULES & NANOPARTICLES

**Baptiste Auguié, Eric Le Ru**  
Victoria University of Wellington, NZ  
*Thanks: Brendan Darby, Matthias Meyer*

# COUPLED DIPOLES IN NANO-OPTICS: SELECTED TOPICS

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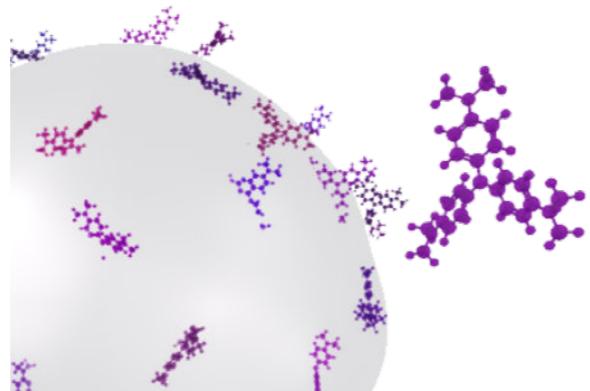
PARTICLE ARRAYS



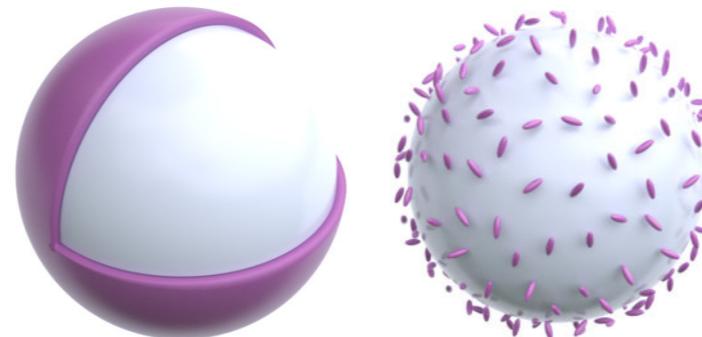
CHIRAL NANO-CLUSTERS



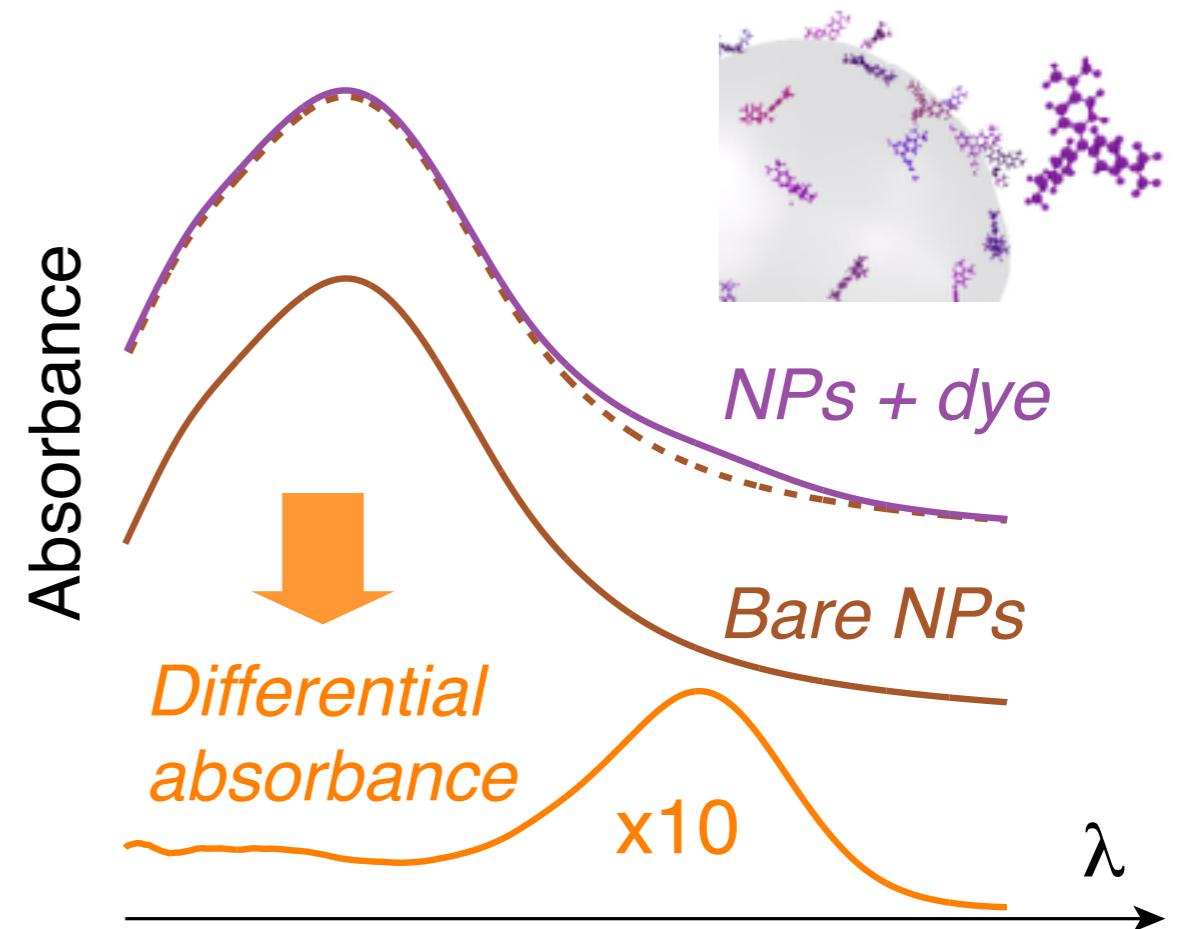
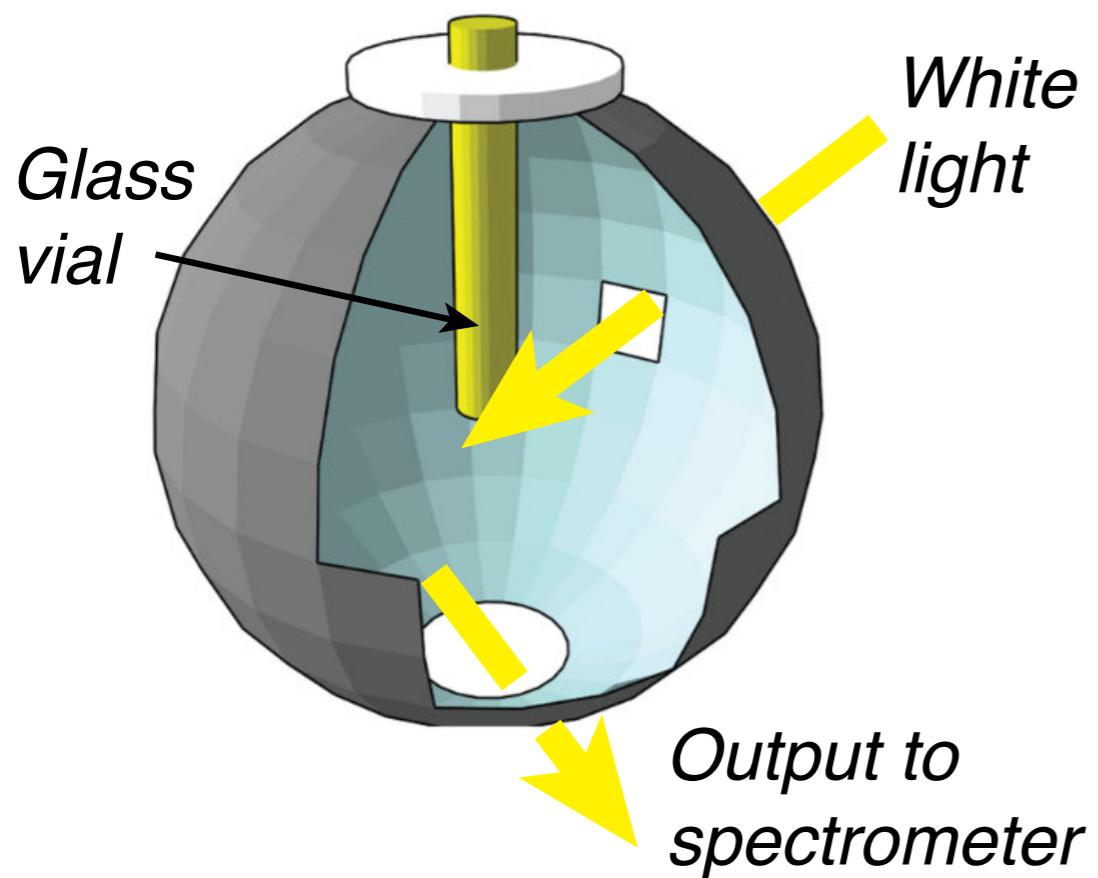
MOLECULES ON COLLOIDS



CORE-SHELLS OF INTERACTING DYES

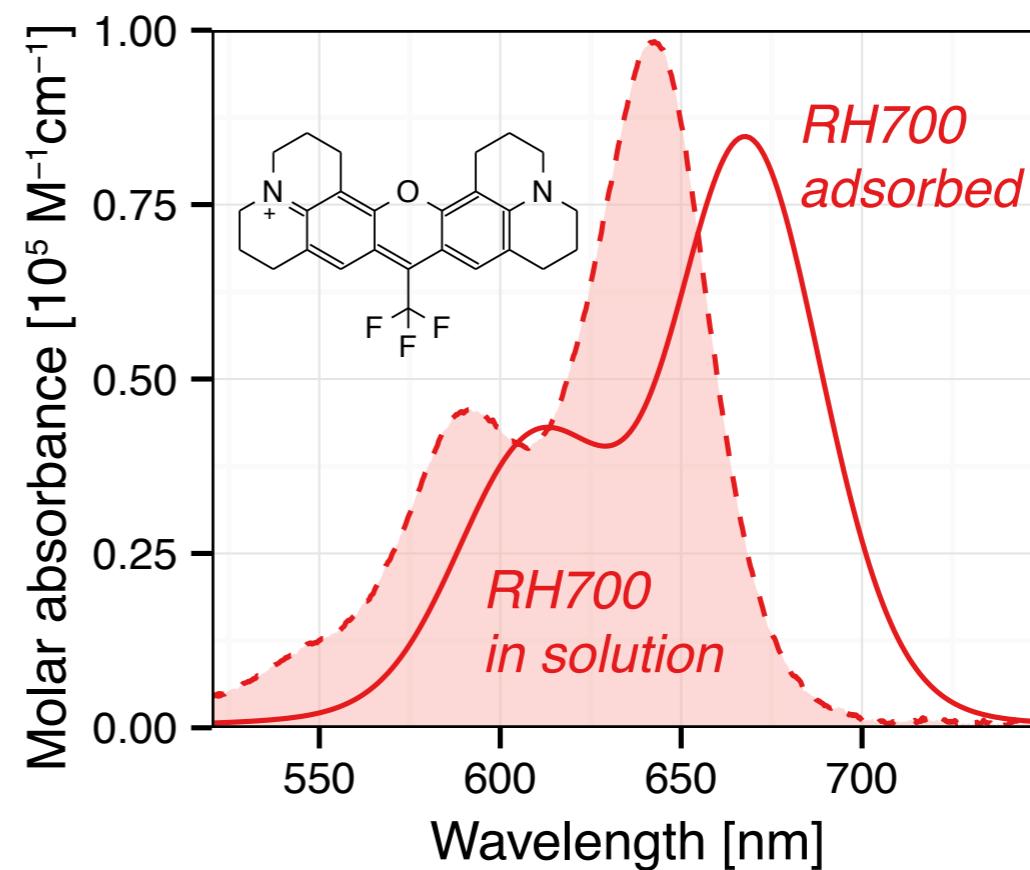
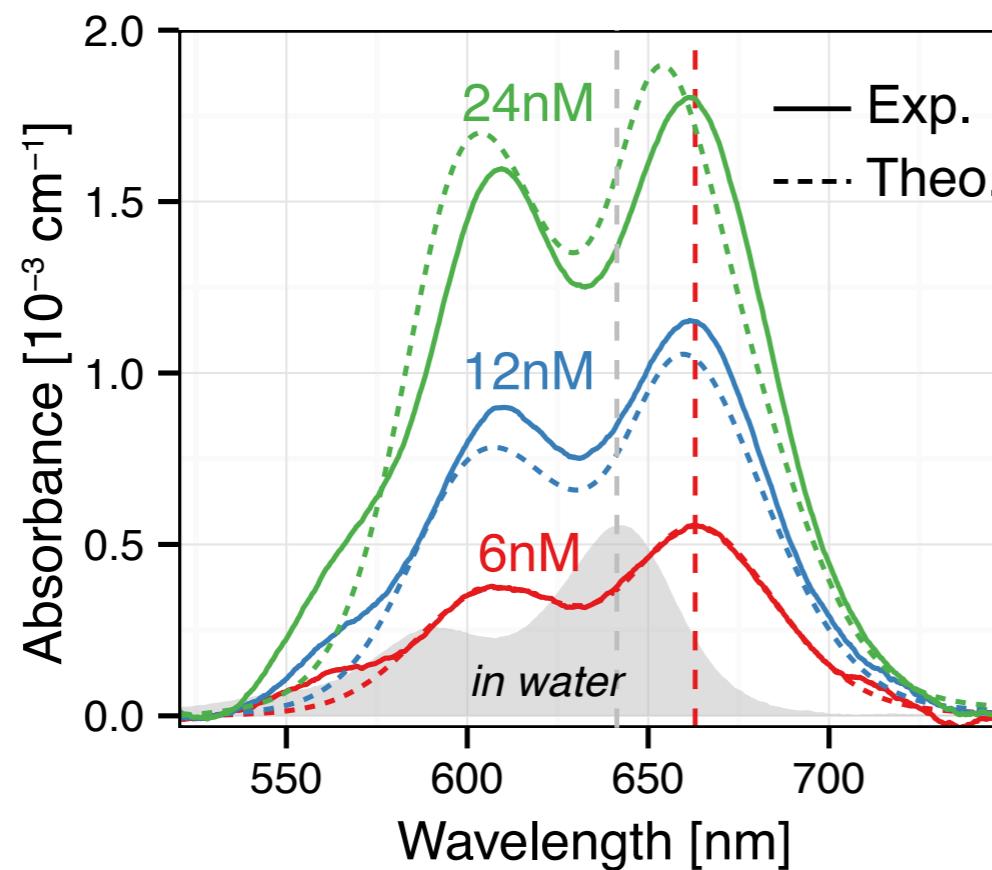
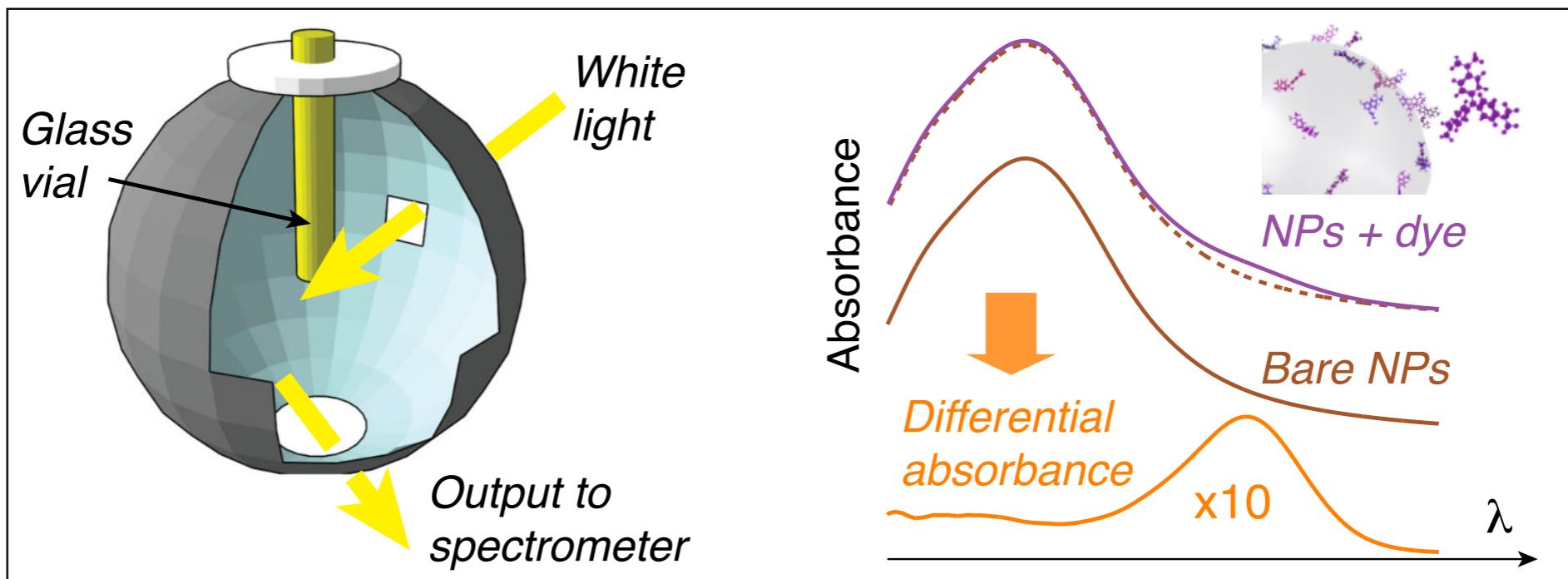


# INTEGRATING SPHERE FOR ABSORPTION MEASUREMENTS

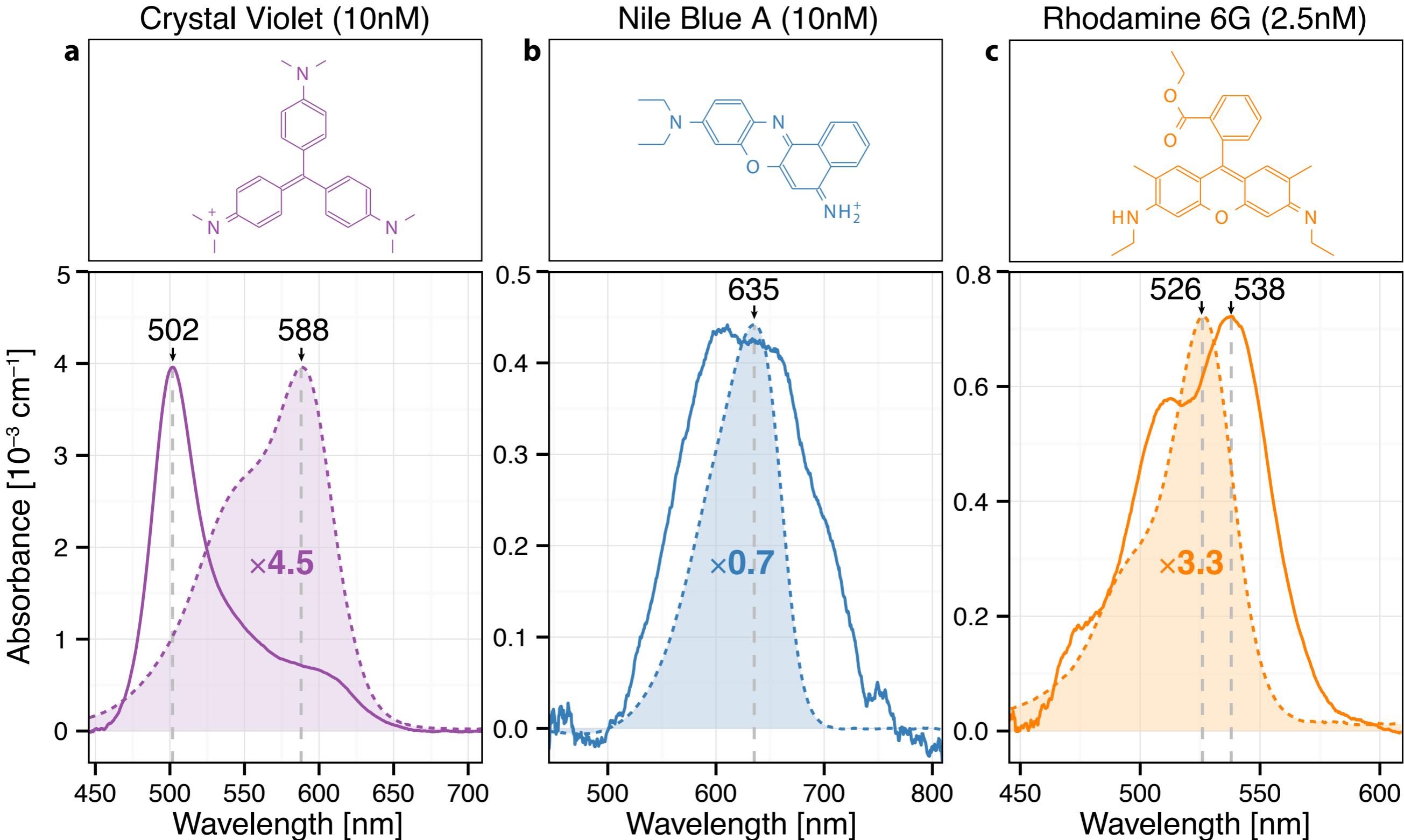


B. L. Darby, B. Auguié, M. Meyer, A. E. Pantoja, and E. C. Le Ru  
*Nat. Photonics* **10**.1 (2016), pp. 40–45

# ABSORPTION OF DYES ON METAL COLLOIDS



# DIFFERENT MOLECULES



# WHAT WE WANT TO KNOW

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- ▶ “Chemical enhancement” / EM (“image dipole”) effect?
- ▶ Implications for Raman and fluorescence
- ▶ What concentration is low enough to avoid interactions?
- ▶ Surface dimerisation?
- ▶ Orientation effects

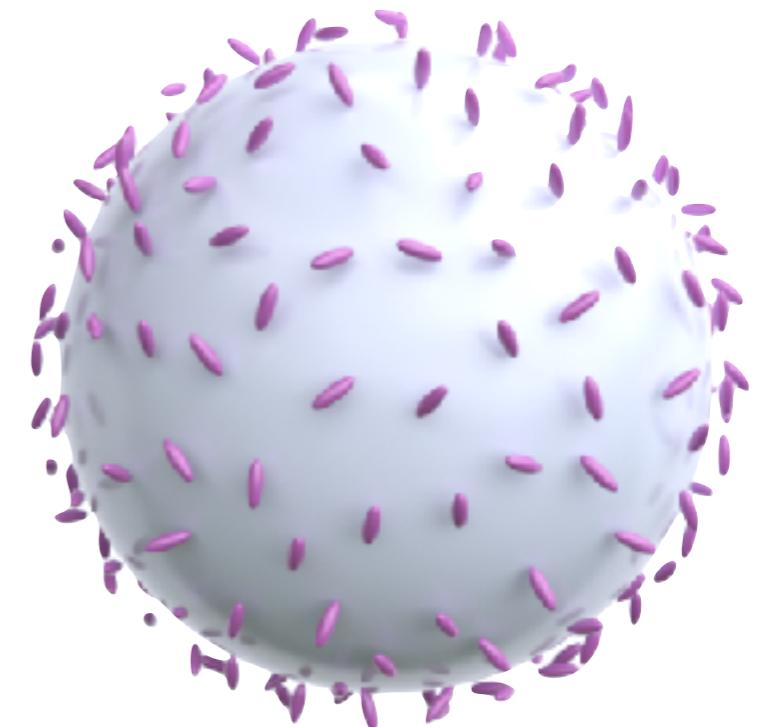
# (NAÏVE) EFFECTIVE-MEDIUM SHELL MODEL

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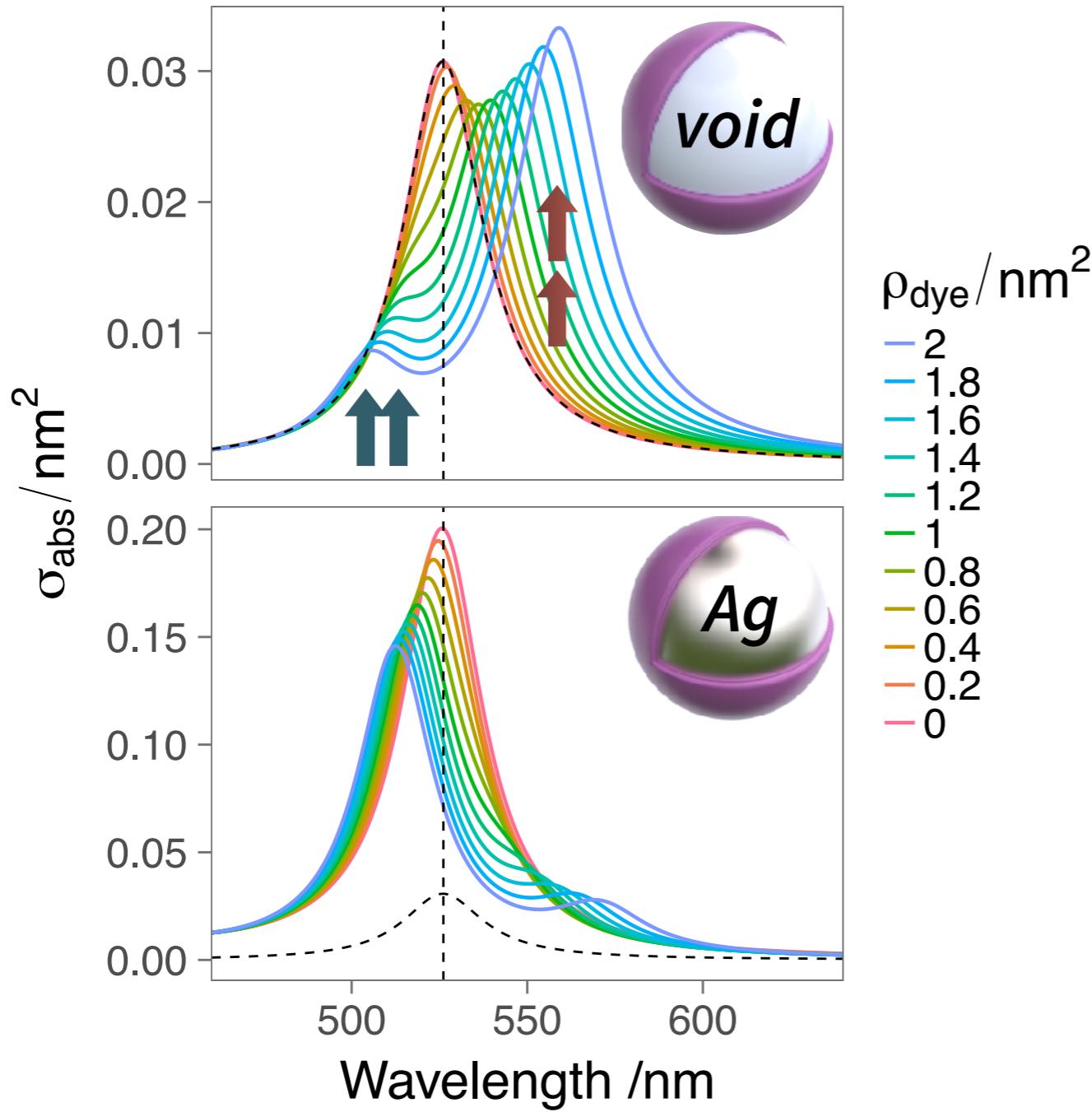
- ▶ Clausius–Mossotti  $\alpha \approx \epsilon$
- ▶ Concentration dependence
- ▶ Local field enhancement

## *Challenges & limitations*

- ▶ CM for bulk, not for 2D shell...
- ▶ Anisotropy, orientation
- ▶ Inhomogeneities  
( $\sim 100$  dyes/colloid @  $1nM$ )
- ▶ Dipole image?

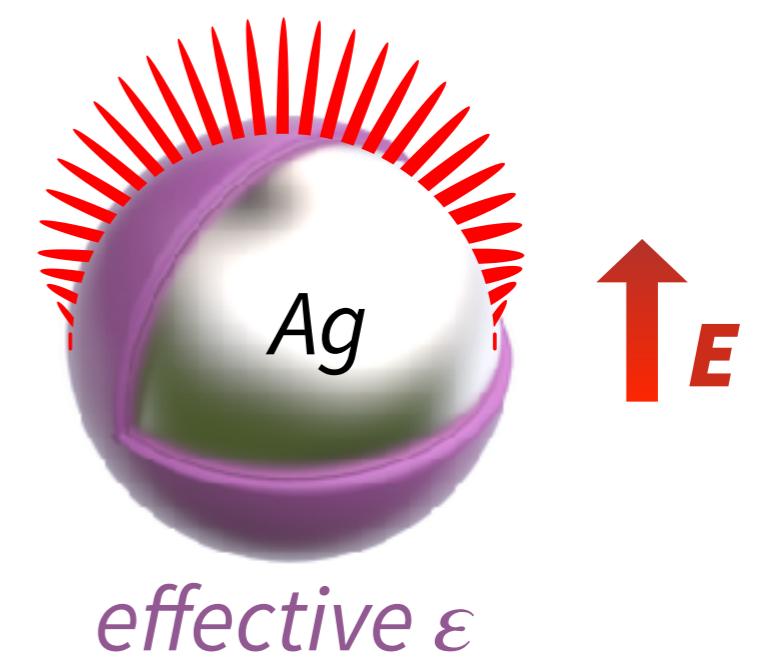


# (NAÏVE) EFFECTIVE-MEDIUM SHELL MODEL



*First insights:*

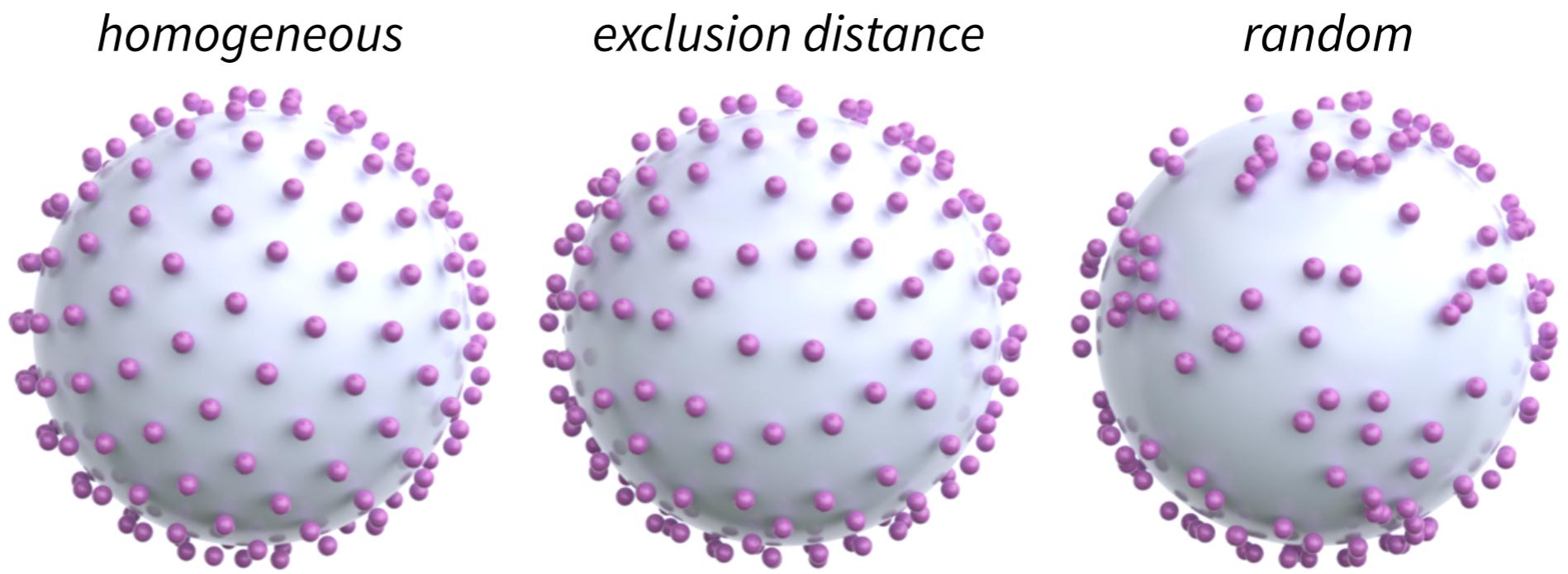
- ▶ Shifts & splitting
- ▶ Local field:  
*enhancement or “quenching”*



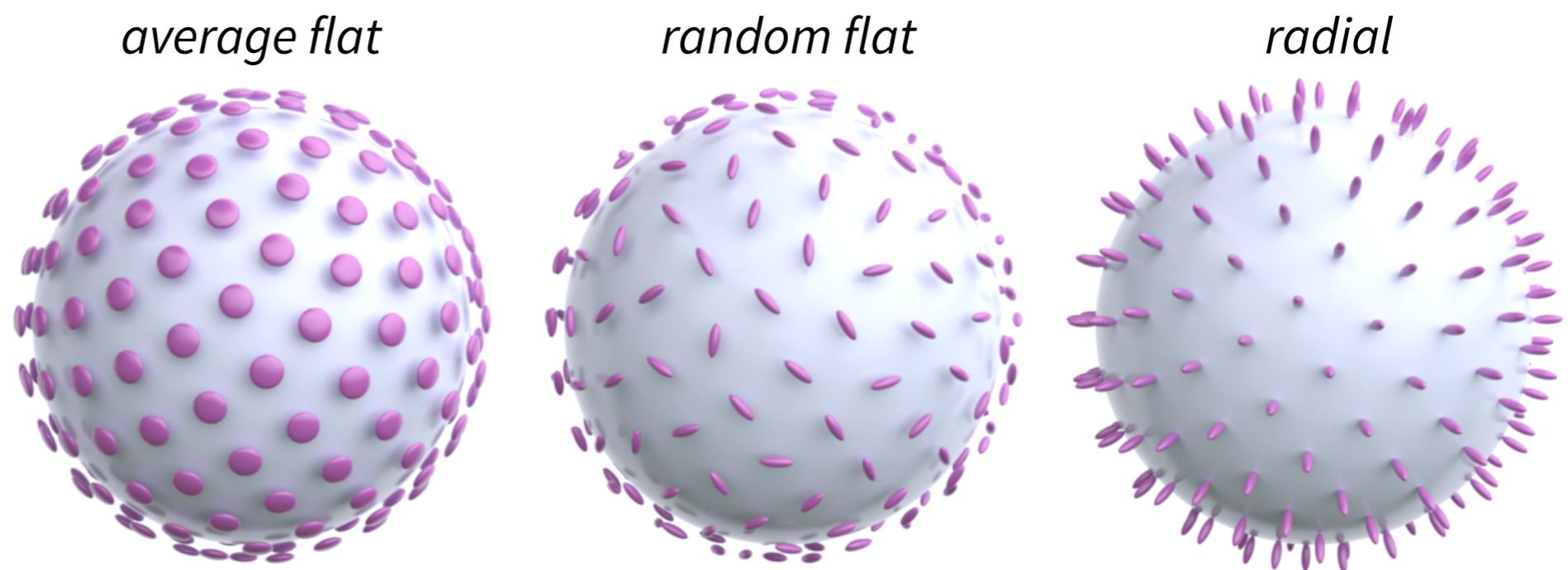
# BEYOND HOMOGENEOUS ISOTROPIC SHELLS

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- Position

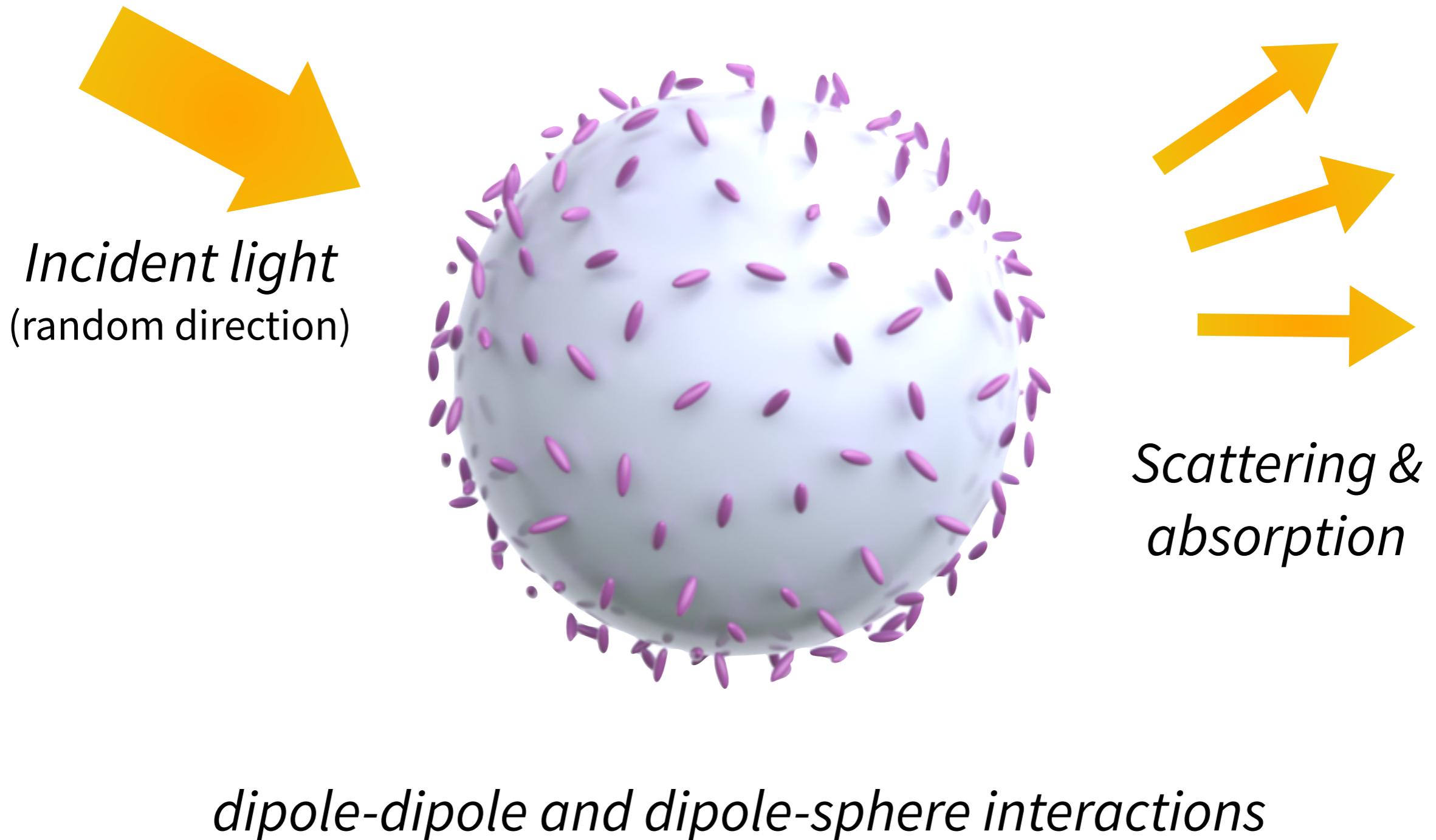


- Orientation

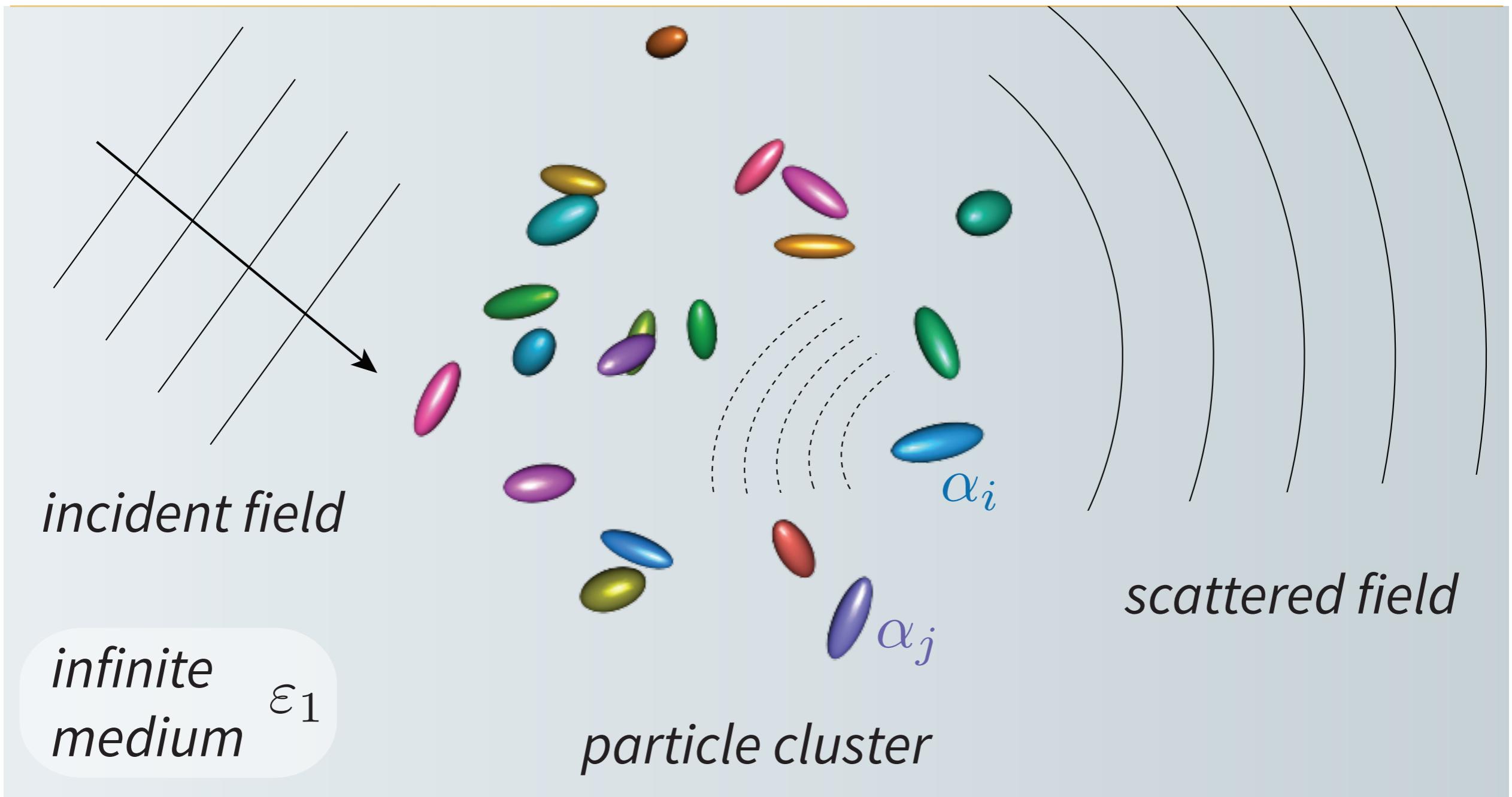


# LIGHT SCATTERING PROBLEM

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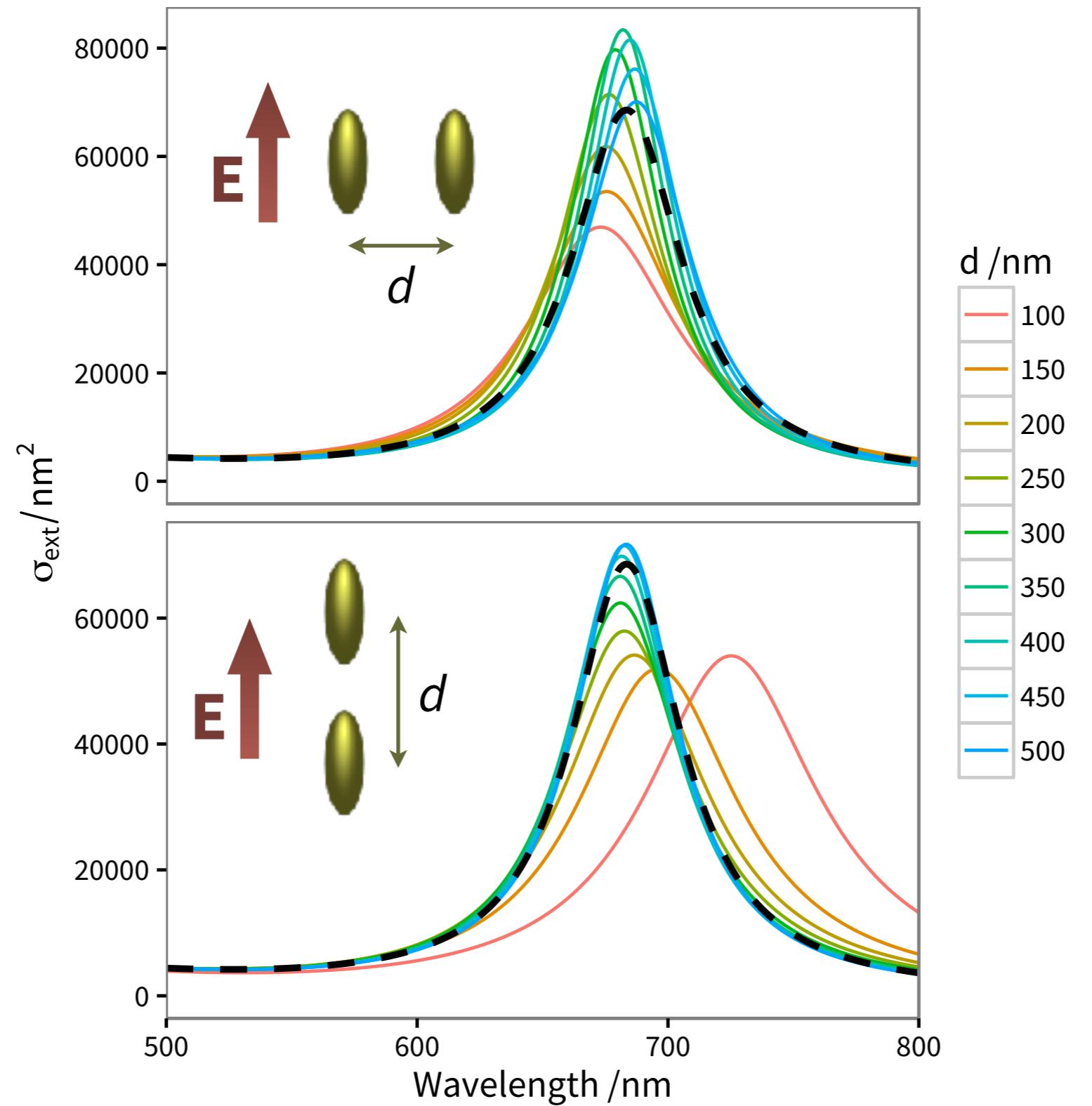


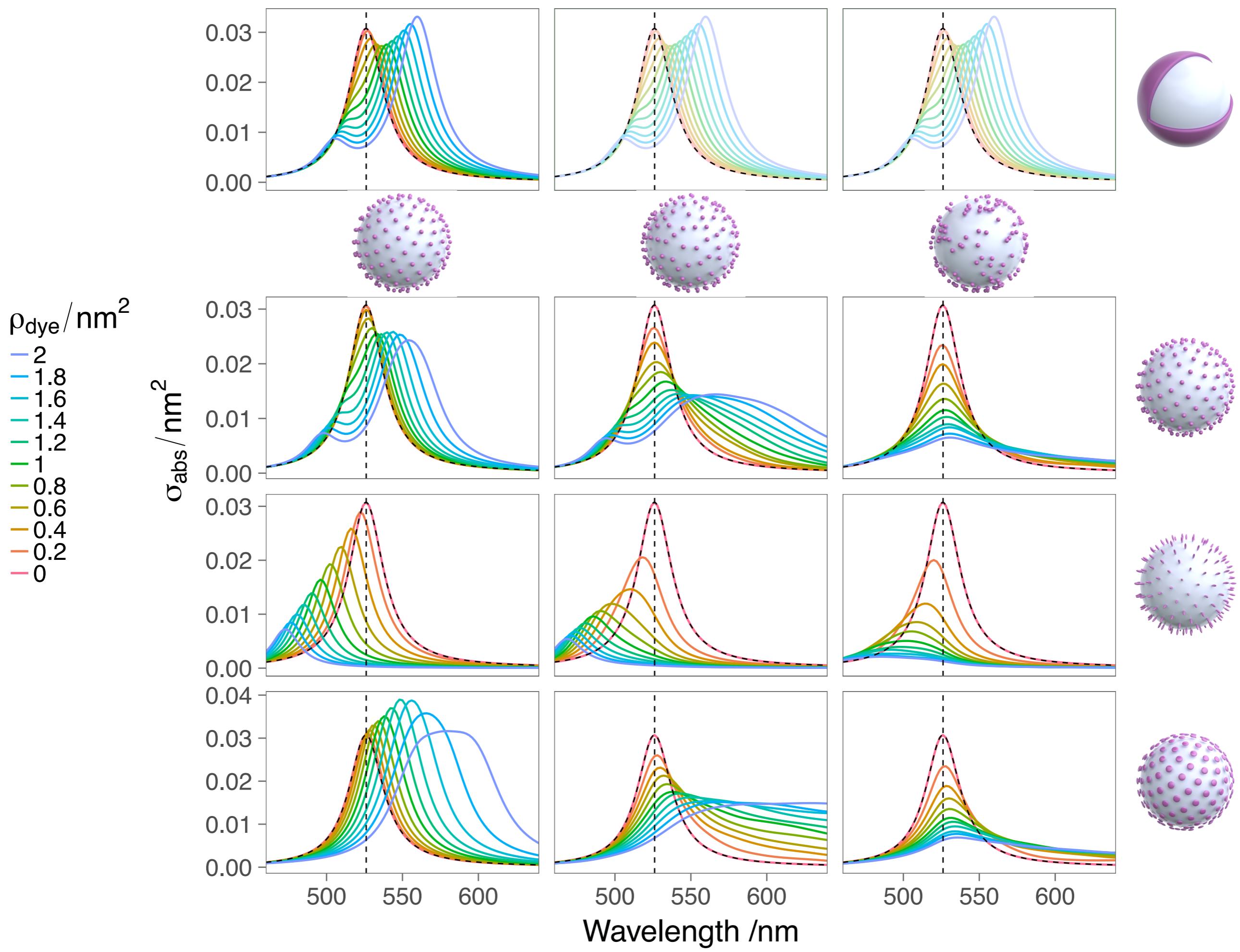
# COUPLED DIPOLE EQUATIONS (NO SPHERE)



$$\mathbf{E}^i = \mathbf{E}_{\text{inc}}^i + \sum_{j \neq i} \mathbb{G}_{ij} \alpha_j \mathbf{E}^j$$

## EXAMPLE • PLASMON HYBRIDISATION





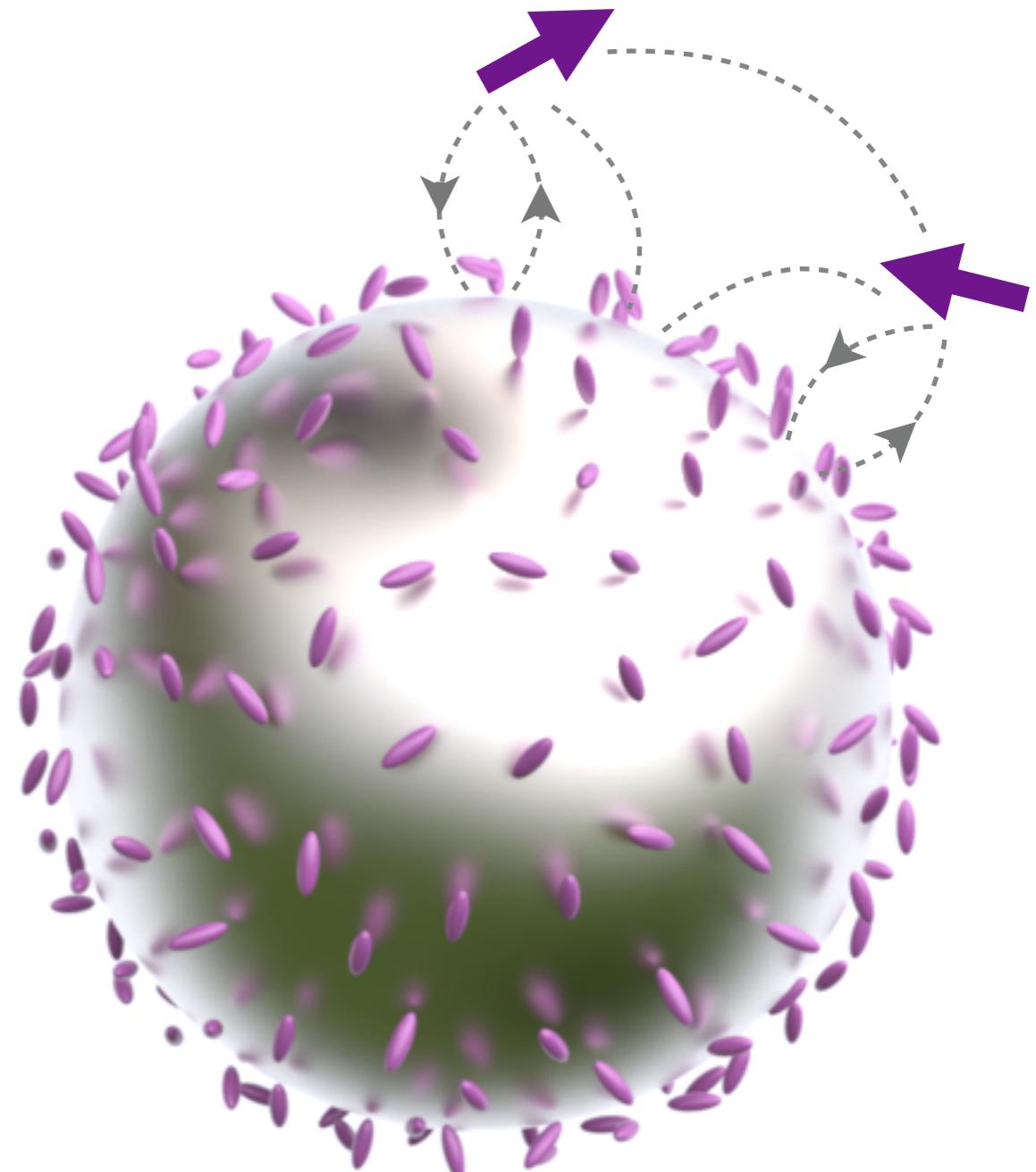
# DIPOLE–SPHERE INTERACTION

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- ▶ Sphere-mediated coupling
- ▶ Self-reaction (“image” dipole)
- ▶ Additional excitation from sphere-scattered field

*Challenges:*

- ▶ Slow convergence of series\*
- ▶ Easier when source along z-axis:  
→ *many rotations!*



\* M. Majić, B. Auguié, E. Le Ru • Phys. Rev. E **95**, 033307 (2017)

## INTERLUDE: HYBRID COUPLED-DIPOLE – MIE THEORY

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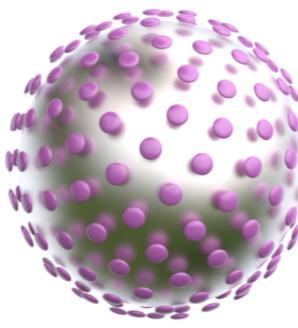
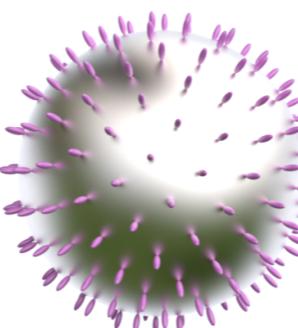
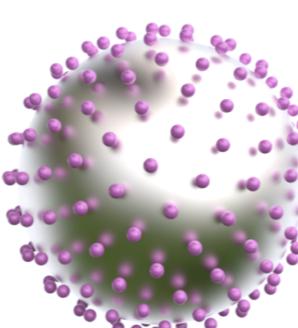
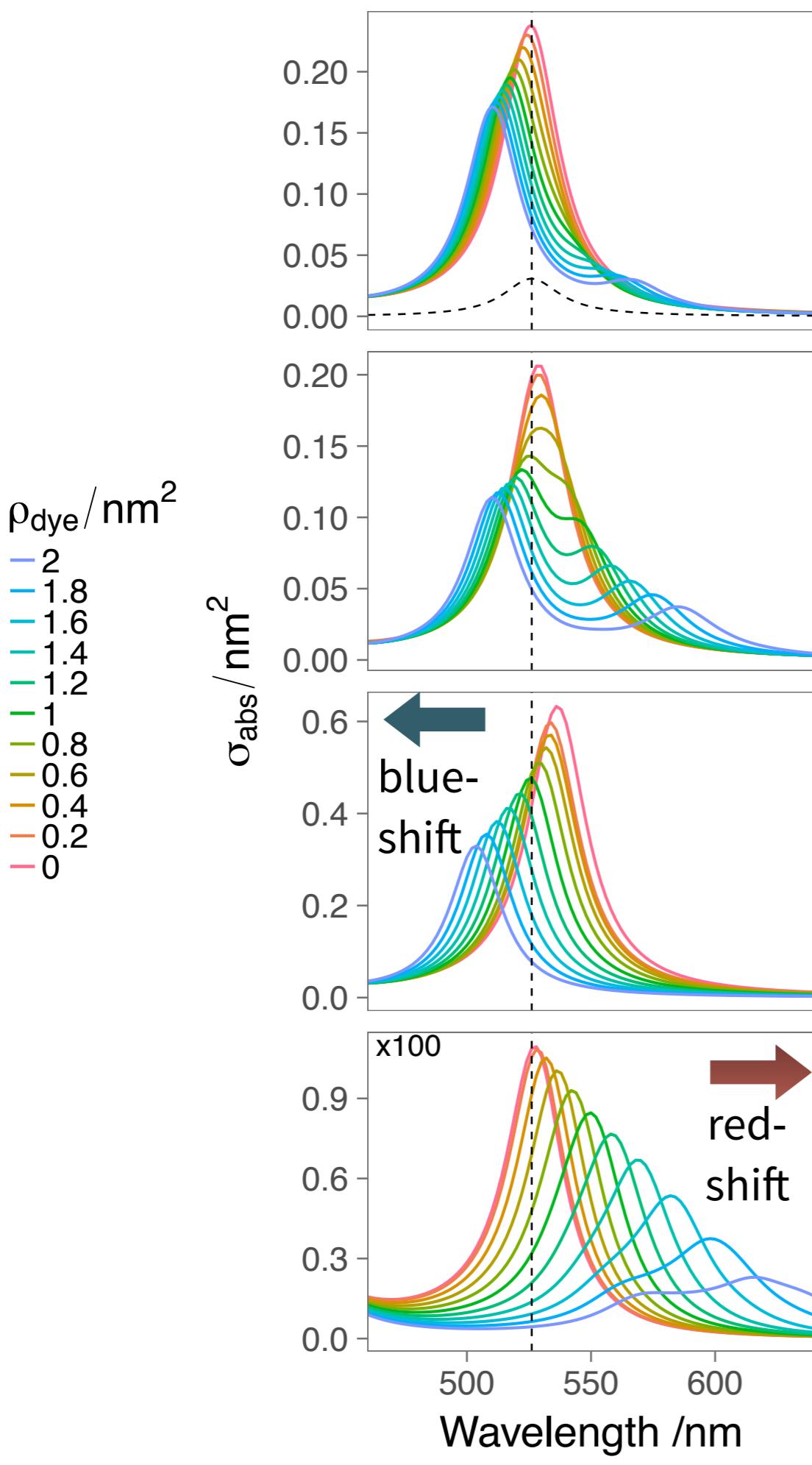
- Extended coupled-dipole system

$$\mathbf{E}^i = \mathbf{E}_{\text{inc}}^i + \mathbf{E}_{\text{SPH}}^i + \sum_{j \neq i} \mathbb{G}_{ij} \alpha_j \mathbf{E}^j + \sum_{\forall j} \mathbb{S}_{ij} \alpha_j \mathbf{E}^j$$

- Cross-sections: Mie theory with  $N+1$  sources

$$\begin{cases} \mathbf{E}_{\text{DIP}} = \sum_{n=1}^{\infty} \sum_{m=-n}^n a_{mn}^{\text{DIP}} \mathbf{M}^{(1)}(k_1, \mathbf{r}) + b_{mn}^{\text{DIP}} \mathbf{N}^{(1)}(k_1, \mathbf{r}), & r < r_{\text{dip}} \\ \mathbf{E}_{\text{DIP}} = \sum_{n=1}^{\infty} \sum_{m=-n}^n e_{mn}^{\text{DIP}} \mathbf{M}^{(3)}(k_1, \mathbf{r}) + f_{mn}^{\text{DIP}} \mathbf{N}^{(3)}(k_1, \mathbf{r}), & r > r_{\text{dip}} \end{cases}$$

- Orientation-averaging (multiple directions)

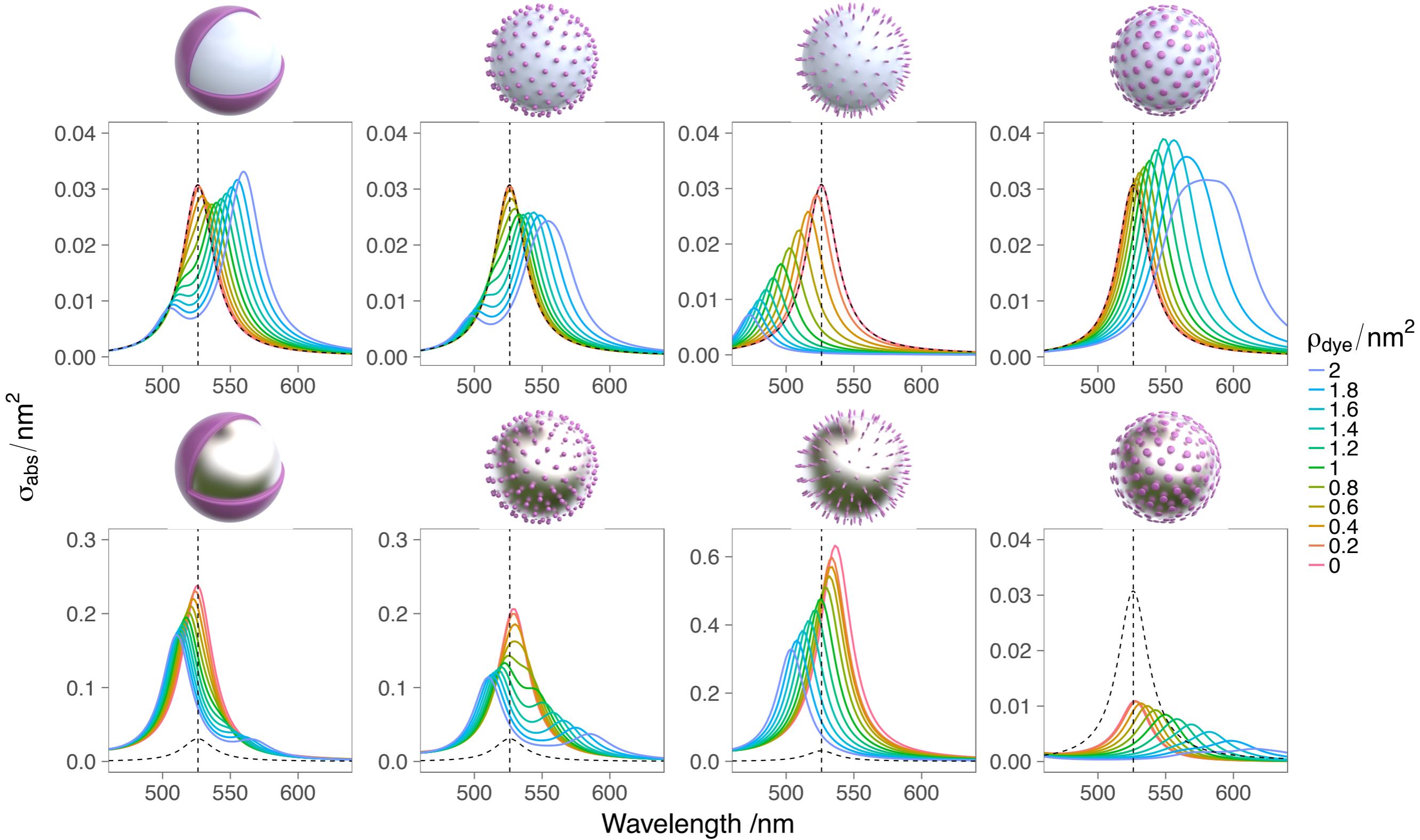


## *First insights:*

- CM  $\approx$  isotropic shell
- Blue-shift: radial
- Red-shift: flat
- Image dipole shift

Note:  $R$ -dependence  
(here 15 nm radius)

# EFFECT OF METAL CORE



## PERSPECTIVES

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- Effect of orientation, density, inhomogeneities, dipole image
- Comparison with anisotropic shell models
- Shell of finite thickness, unusual coverage (e.g. Janus)
- Surface dimerisation
- Implications for Raman and fluorescence

*Less likely:*

- Chemical enhancement*, DFT predictions
- Super-radiance
- Non-spherical particles

**THANK YOU!**

